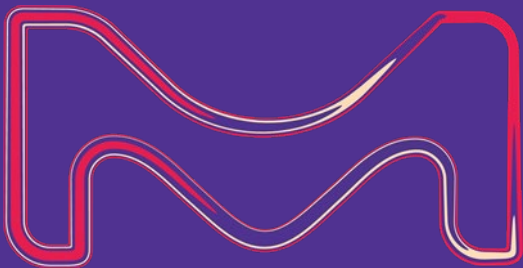


The Electronics business of Merck KGaA, Darmstadt, Germany
operates as EMD Electronics in the U.S. and Canada.

Differentially private Federated learning for High-accuracy carbon Footprint prediction

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EMD
ELECTRONICS

Using Machine Learning in Carbon Footprint Prediction

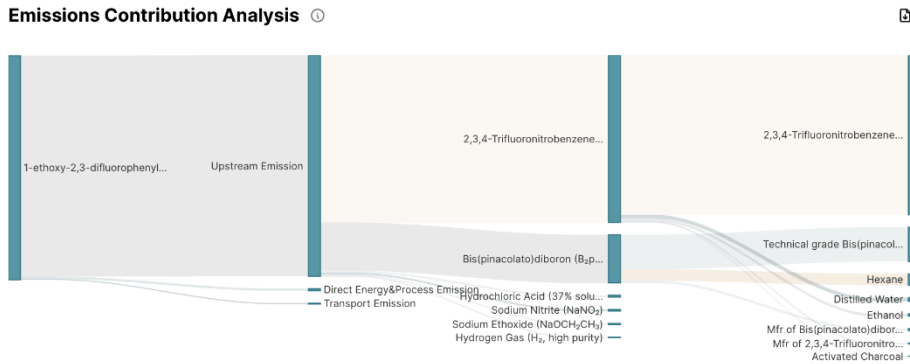


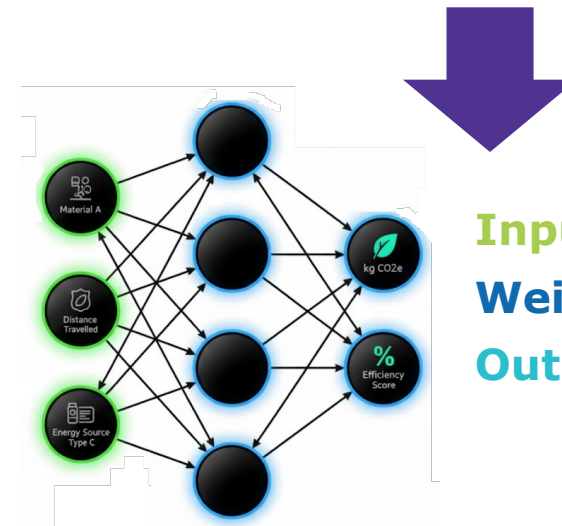
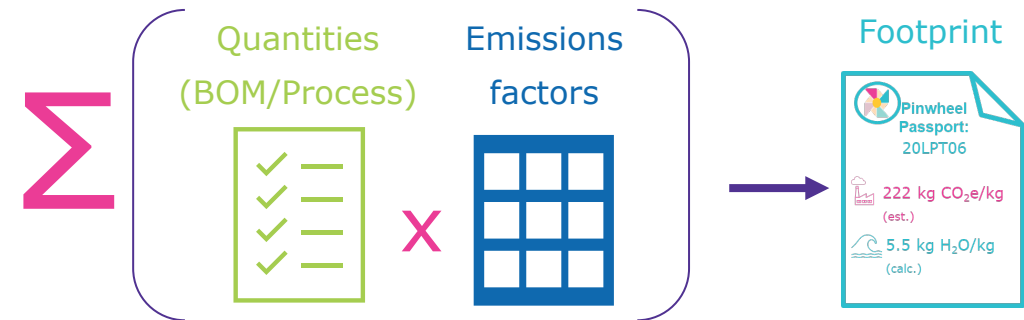
image generated from Muir AI PCF analysis

Environmental footprint reporting and sustainable design requires **tracing inputs across complex supply chains**.

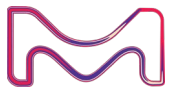
Currently, a lack of data hampers accurate calculations:

- Most emissions **databases cover only a small fraction** of known materials.
- **Proprietary processes** and inputs restrict data availability.

Recasting **footprint calculation as a deep learning problem** enables accurate, scalable, and privacy-preserving predictions.



Inputs: Quantities
Weights: Factors
Outputs: Footprints



Differentially Private Federated Learning (DPFL) Framework

Federated learning

Aggregate the models , not the data from different clients

Differential privacy

Add a little noise to the model updates to hide the true updates in the FL framework

Algorithm 1 Differentially Private Federated Learning (DPFL)

Input: Datasets $\{D_i\}_{i \in [m]}$ belonging to m clients, initial baseline model θ_b , target privacy budget (ϵ, δ) , number of local epochs E , learning rate η , the number of round T

Output: Differentially private global model $\bar{\theta}$

for each round $t = 1, 2, \dots, T$ **do**

for each client $i \in [m]$ in parallel **do**

 Receive global model θ_b from the server

 Compute noisy local gradient updates:

$\tilde{g}_i = \text{LocalTrain}(\theta_b, D_i, E, \eta, \frac{\epsilon}{Tm}, \frac{\delta}{Tm})$

 Send $\tilde{g}_i$ to the server

end for

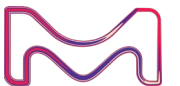
 Aggregate noisy gradients at the server:

$\Delta = \frac{1}{m} \sum_{i \in \mathcal{S}} \tilde{g}_i$

 Update global model: $\theta_b \leftarrow \theta_b + \Delta$

end for

Return the final global model $\bar{\theta} = \theta_b$

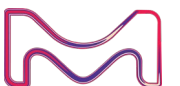


Experimental Results

- **Data source:** Real-world processes from **TianGong** (10k+ LCA unit processes).
- **Emission factors:** Matched with **OpenLCA Nexus** database (kg CO₂ eq/unit).
- **Filtering:** Kept **508 processes** with full material–factor alignment (**97 materials** total).
- **Label computation:** Total footprint = $\Sigma(\text{input} \times \text{emission factors})$
- **Split: 80% training (3 clients), 20% testing.**

ϵ	$R^2(1)$	$R^2(2)$	$R^2(3)$	$R^2(\text{agg})$	$R^2(\text{baseline})$
1.5	0.9775	0.8150	0.4637	0.7709	0.9039
3	0.6969	0.7240	0.8734	0.8976	0.9852
15	0.9952	0.9464	0.9917	0.9608	0.9947
30	0.9990	0.9853	0.9910	0.9789	0.9954

At $\epsilon = 15$, DPFL predicts footprints within 5% of the non-private baseline, striking a strong **balance between privacy and accuracy**.



Together, we can enable
collaborative sustainability.

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