



# AMPHOS<sup>21</sup>

member of  
**RSK**



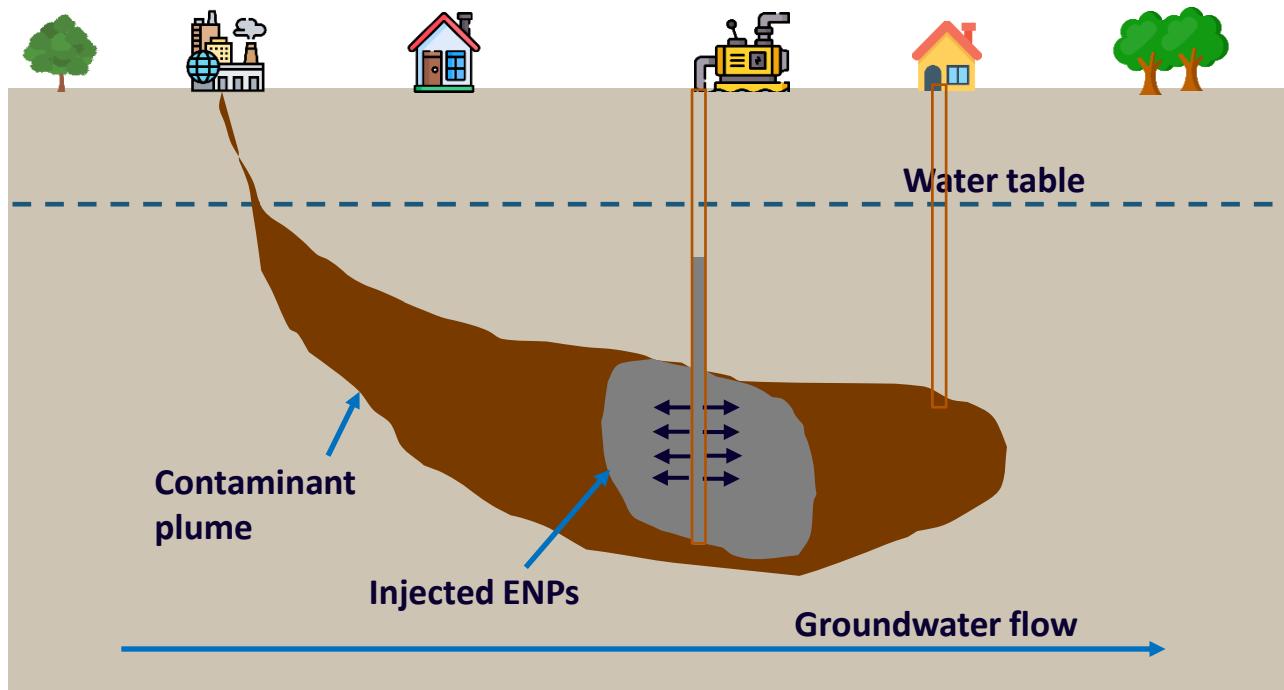
## **Dynamic weights enabled Physics-Informed Neural Network for simulating the mobility of Engineered Nano-particles in a contaminated aquifer**

Shikhar Nilabh, Fidel Grandia

*NeurIPS 2022 Workshop  
Tackling Climate Change with Machine Learning*

# Background

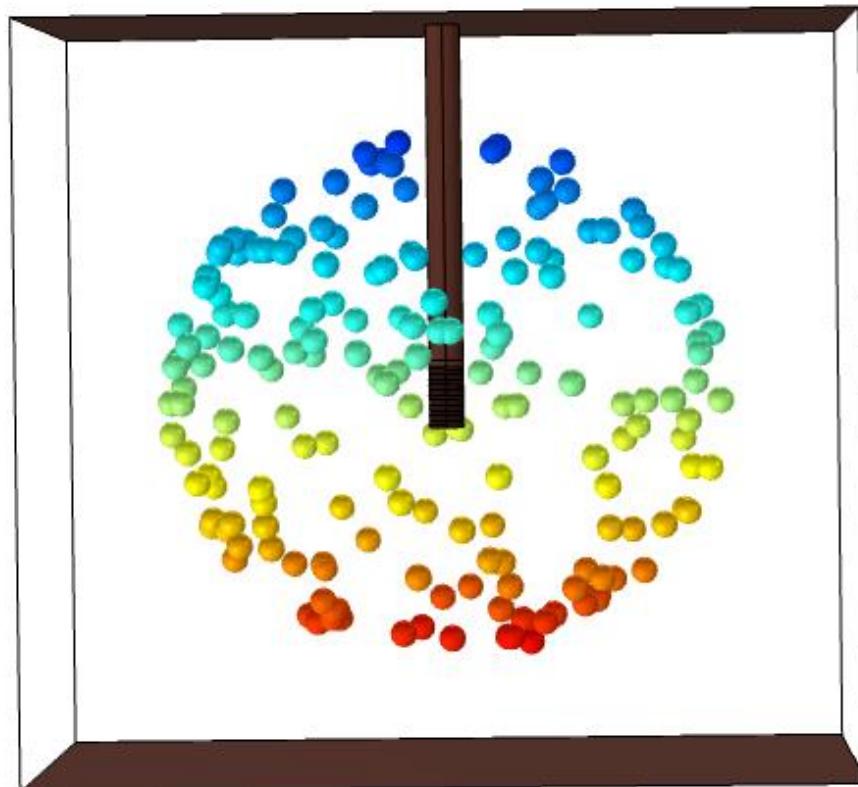
- More than 340000 aquifers are contaminated due to anthropogenic activities just in Europe (Jarsjö et al., 2022)
- The aquifer contamination aggravate climate change due to degradation of soil quality, costal ecosystem and deforestation.
- A promising techniques for remediating the groundwater is by injecting Engineered nano particles (ENPs) that eliminates the contamination



# Groundwater remediation strategy

$$\frac{\partial(\theta c)}{\partial t} + \frac{\partial(s)}{\partial t} = -\nabla(vc) + \nabla((D_e + \propto v)\nabla c)$$

$$\frac{\partial(s)}{\partial t} = \theta k_a c - k_d s$$

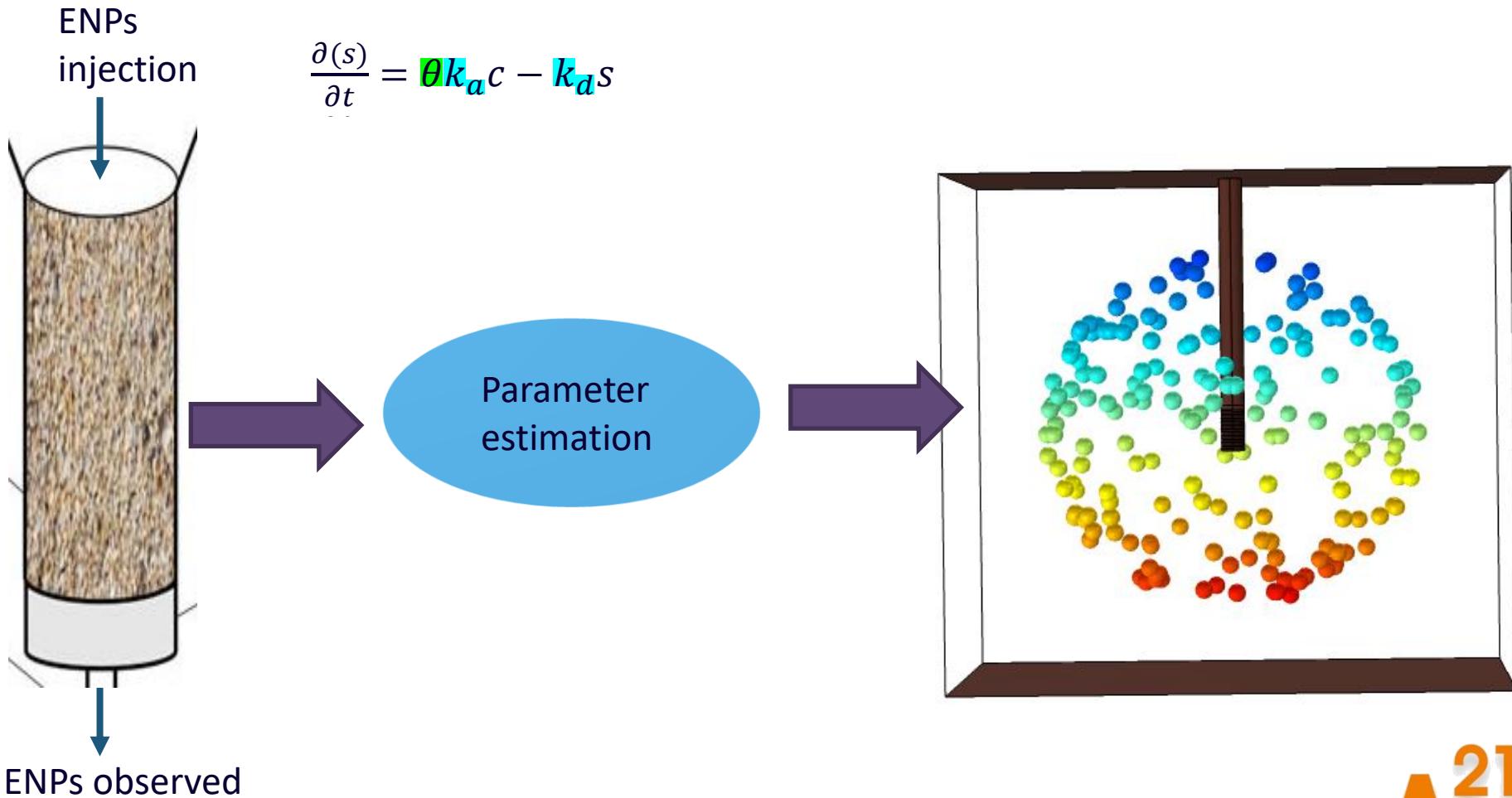


$\theta$ : porosity,  $v$ : flow rate,  $\propto$ : dispersivity,  $c$ : aqueous ENPs,  $s$ : retained ENPs,  $k_a$ : attachment coefficient,  $k_d$ : detachment coefficient

Source of column sand figure: Tan et.al, 2020

# Groundwater remediation strategy

$$\frac{\partial(\theta c)}{\partial t} + \frac{\partial(s)}{\partial t} = -\nabla(vc) + \nabla((D_e + \propto v)\nabla c)$$

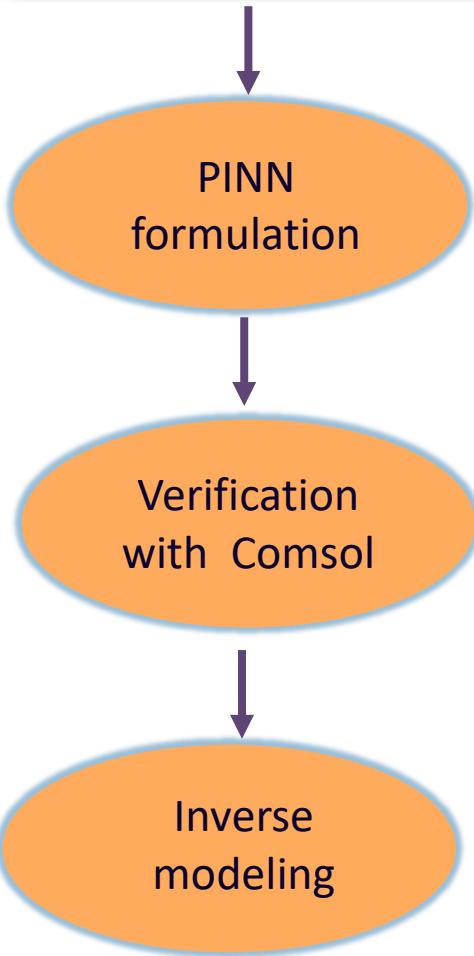


$\theta$ : porosity,  $v$ : flow rate,  $\propto$ : dispersivity,  $c$ : aqueous ENPs,  $s$ : retained ENPs,  $k_a$ : attachment coefficient,  $k_d$ : detachment coefficient

Source of column sand figure: Tan et.al, 2020

# Simulation workflow

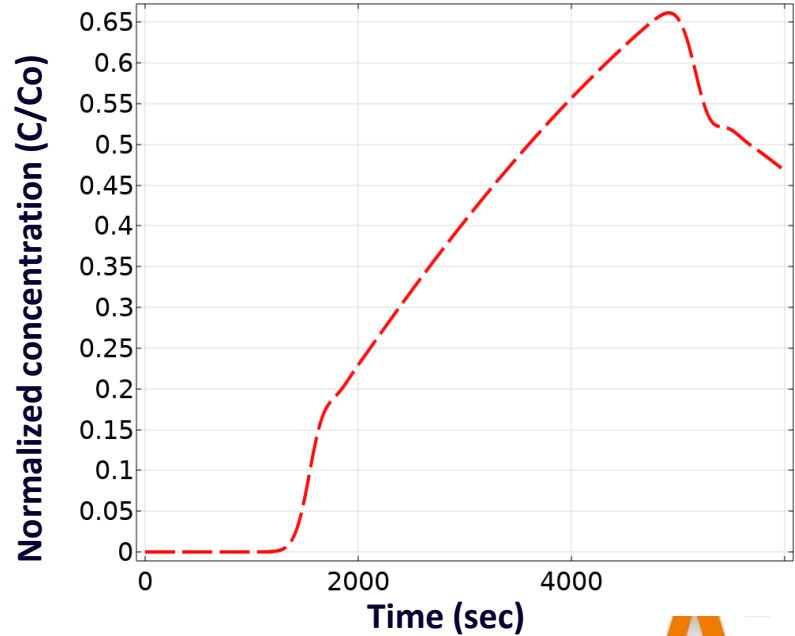
Aim: To develop a simulator for parameter estimation



1D simulated domain  
to estimate:  
 $\theta, \alpha, k_a, k_d$

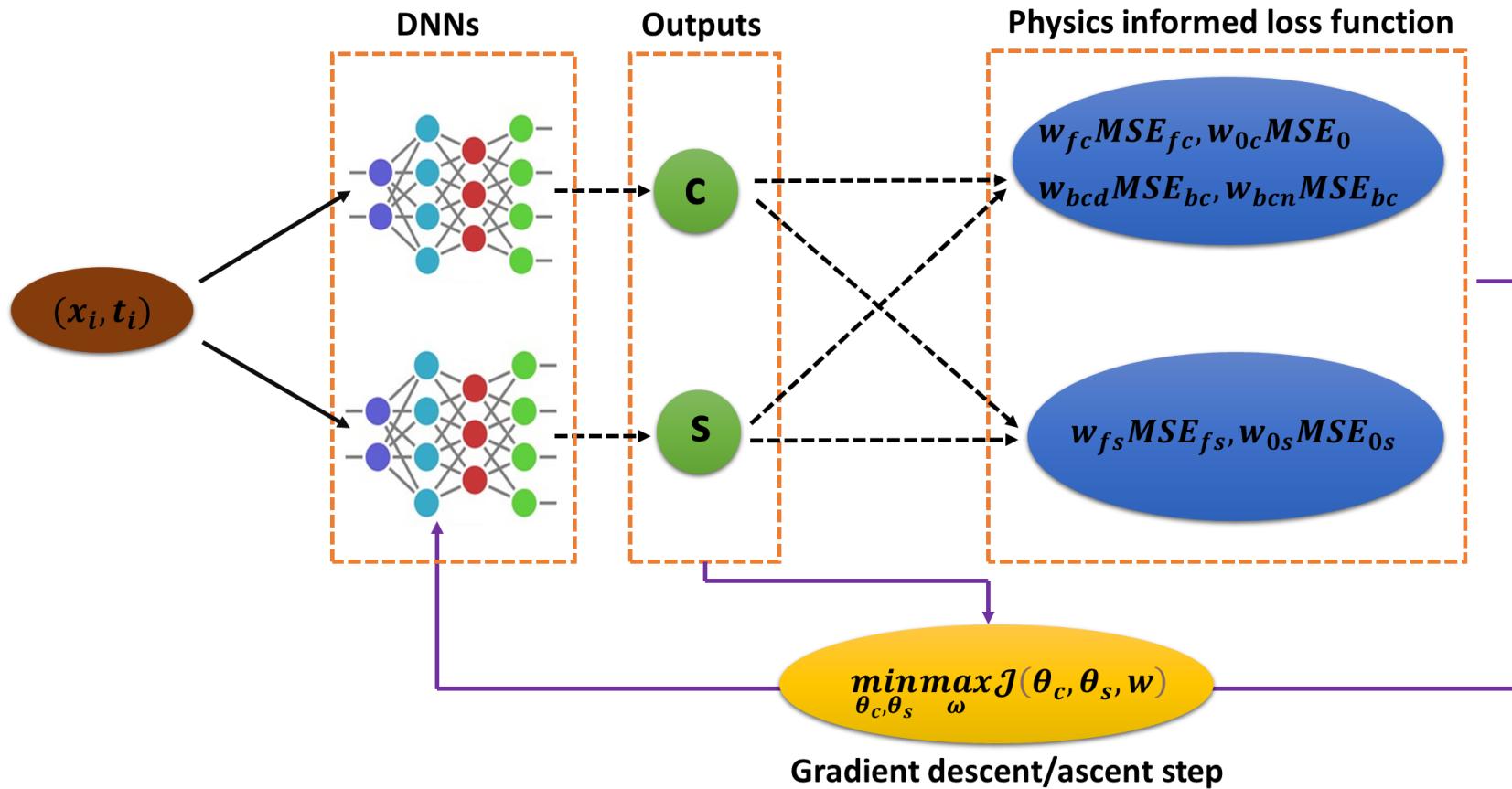
$$\boxed{\begin{aligned} \frac{\partial(\theta c)}{\partial t} + \frac{\partial(s)}{\partial t} &= -\nabla(vc) + \nabla((D_e + \alpha v)\nabla c) \\ \frac{\partial(s)}{\partial t} &= \theta k_a c - k_d s \\ c(0, t) &= \left( \frac{1}{1 + e^{-0.02(t-500)}} \right) \times \left( \frac{1}{1 + e^{0.02(t+500)}} \right) \\ \nabla((D_e + \alpha_L v)\nabla c(1, t)) &= 0 \\ c(x, 0) = s(x, 0) &= 0 \end{aligned}}$$

*Second Inverse model:*  
 $\theta = \checkmark \quad \alpha = \checkmark \quad k_a = ?, \quad k_d = ?$



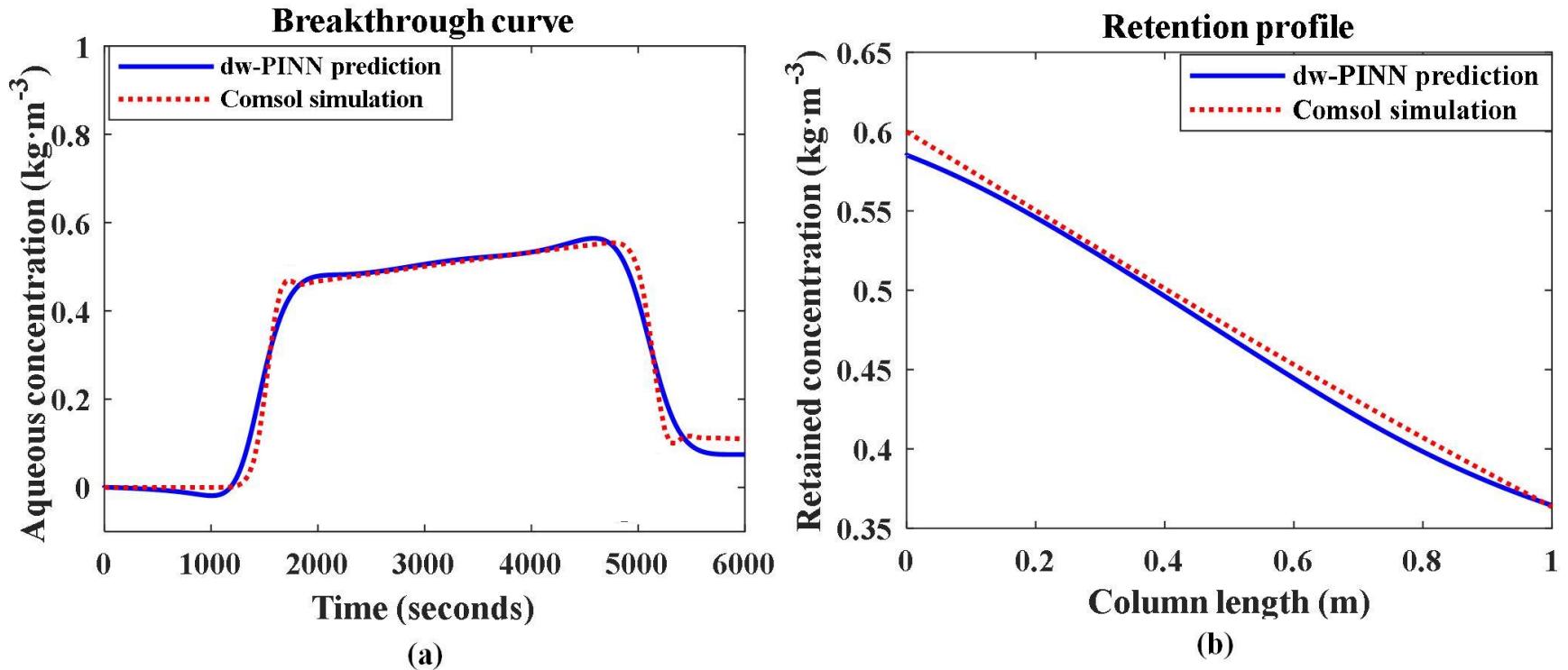
A

# Applied PINN framework



Flowchart of dw-PINN framework representing two Deep Neural Networks with time and spatial points as input and concentration of aqueous and retained ENPs as output

# Stage 1: Forward modeling verification

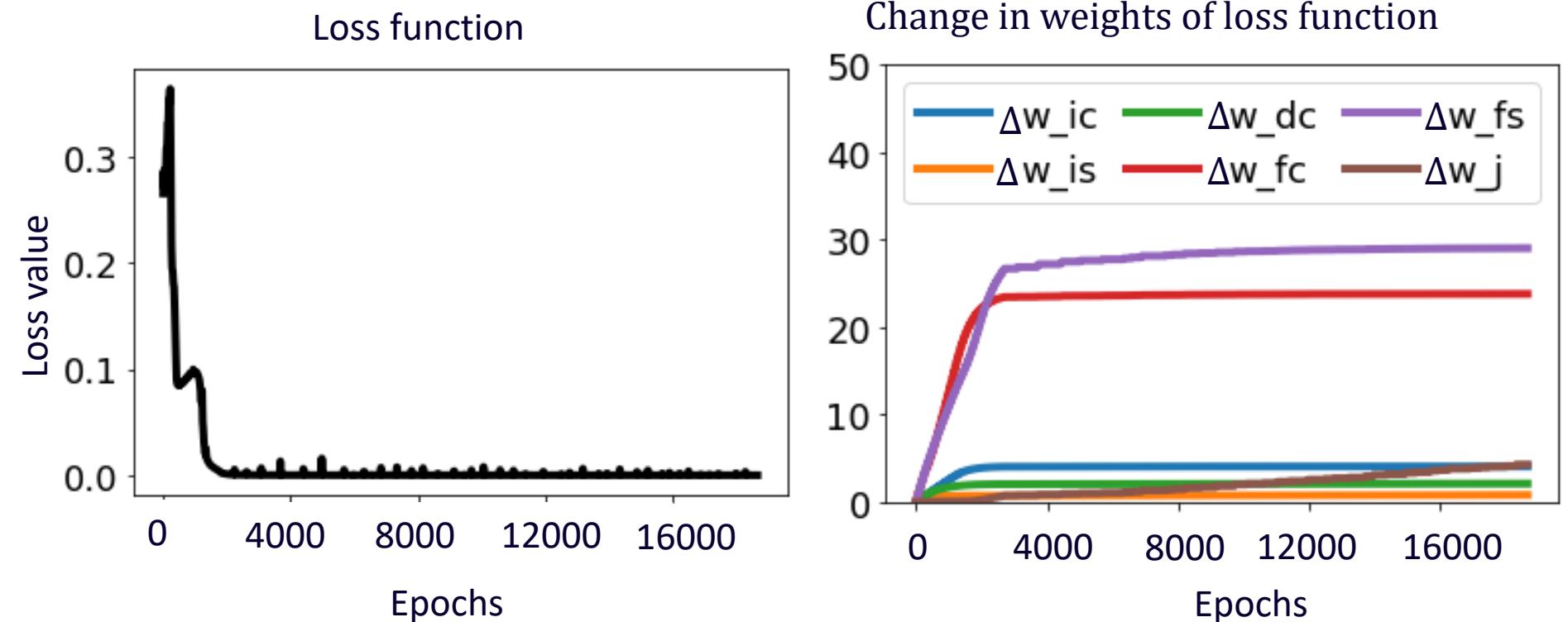


Result comparison of dw-PINN and Comsol model; (a) breakthrough curve (b) retention profile

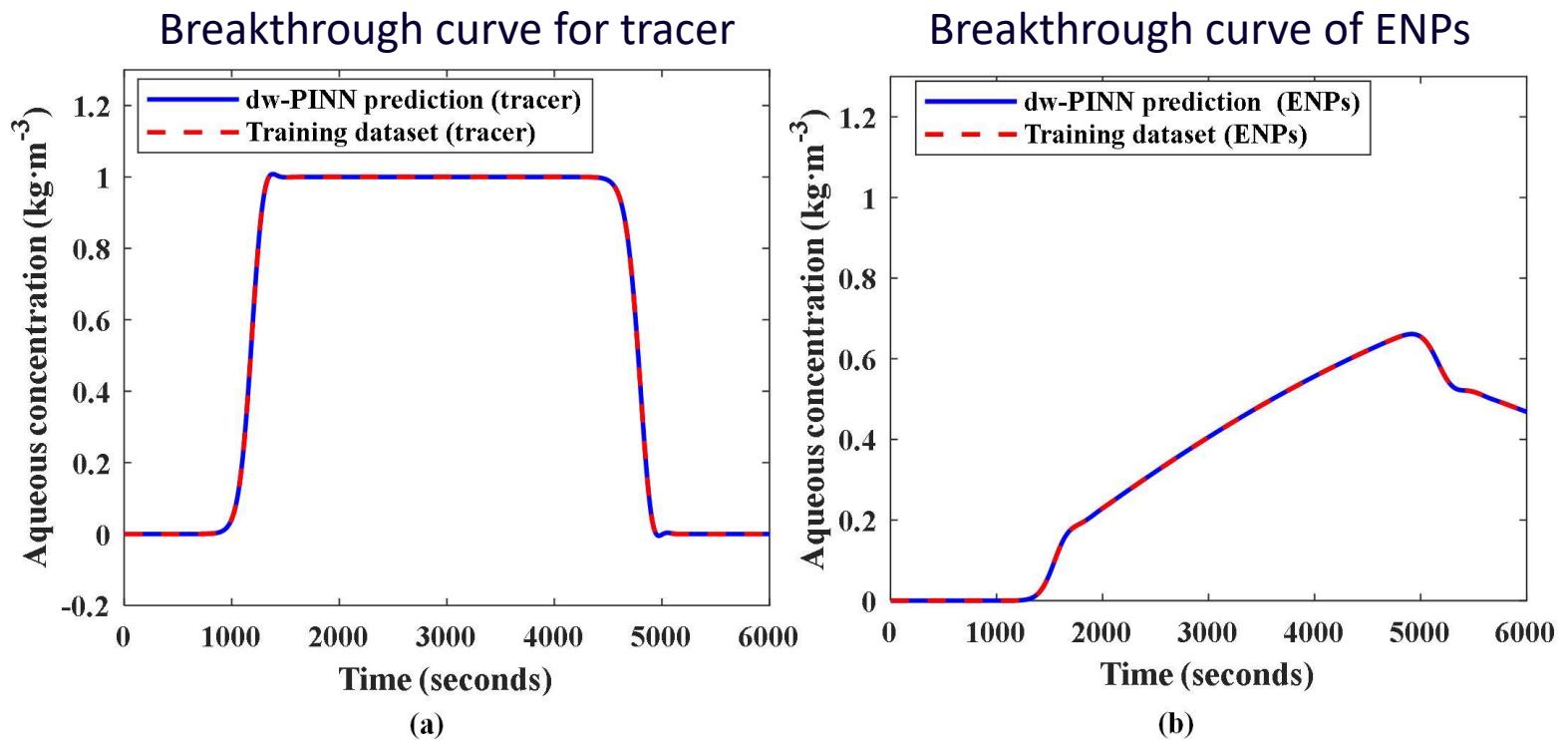
$$v = 0.0003 \text{ m}\cdot\text{s}^{-1}, D_e = 1\text{e}-9 \text{ m}^2\cdot\text{s}^{-1}, \alpha = 0.01, k_a = 0.00008 \text{ s}^{-1}, k_d = 0.0001 \text{ s}^{-1}, \theta = 0.3,$$

Column length = 1 m

## Stage 1: Loss function and Dynamic weights



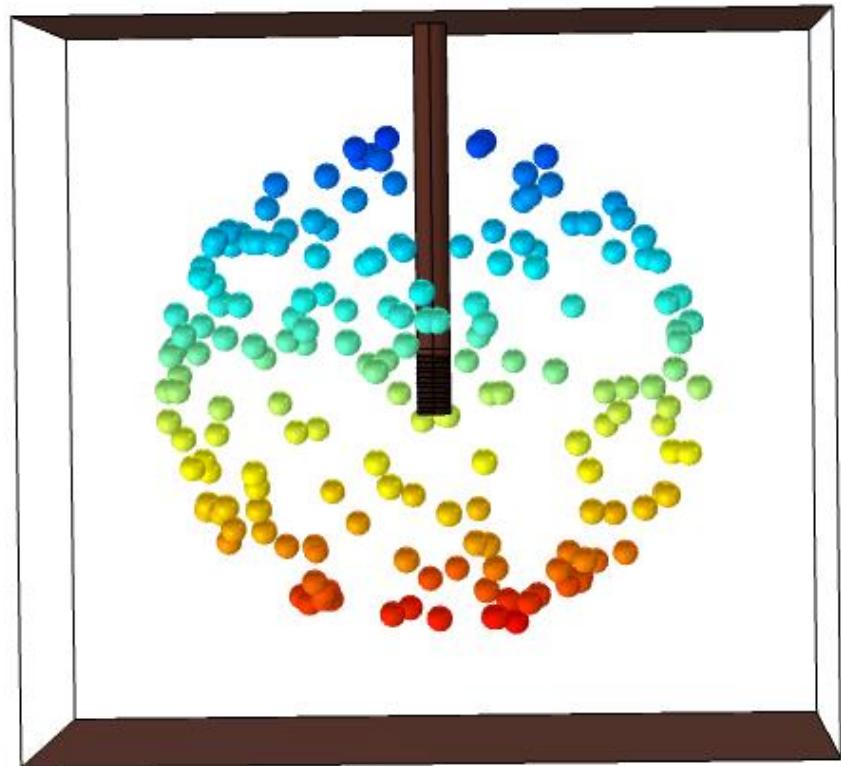
## Stage 2: values estimated and comparison



|                  | Porosity | Dispersivity (m) | Attachment Coefficient ( $\text{s}^{-1}$ ) | Detachment coefficient ( $\text{s}^{-1}$ ) |
|------------------|----------|------------------|--|--|
| Ground truth     | 0.20     | 0.0050           | 0.00070                                    | 0.00010                                    |
| Estimated values | 0.21     | 0.0059           | 0.00071                                    | 0.00018                                    |

## Conclusion and future work

- The model result matches well with the benchmark cases from the numerical simulator, Comsol Multiphysics
- The result demonstrates that the PINN based simulation tool is a viable option for parameter estimations required for upscaling
- Application of simulation tool on real 1D sand-filled column data & forward modeling on 3D system is being explored



Development of ENP's mobility in a 3D system

# AMPHOS<sup>21</sup>



## ESPAÑA

C. Venezuela, 103, 2<sup>a</sup> planta  
08019 Barcelona  
Tel.: +34 93 583 05 00

Paseo de la Castellana 40, 8<sup>a</sup> Planta  
28046 Madrid  
Tel.: +34 620634729

## CHILE

Avda. Nueva Tajamar, 481  
WTC – Torre Sur – Of 1005  
Las Condes, Santiago  
Tel.: +562 2 7991630

## PERÚ

Av. Primavera 785, Int. 201,  
Urb. Chacarilla - San Borja  
Lima 41  
Tel.: +51 1 592 1275

[www.amphos21.com](http://www.amphos21.com)



member of

# RSK

[www.rskgroup.com/rsk-businesses/](http://www.rskgroup.com/rsk-businesses/)