



# Stable RL for Voltage Control

Using Reinforcement learning for Real-time Voltage  
Control in Distribution Systems

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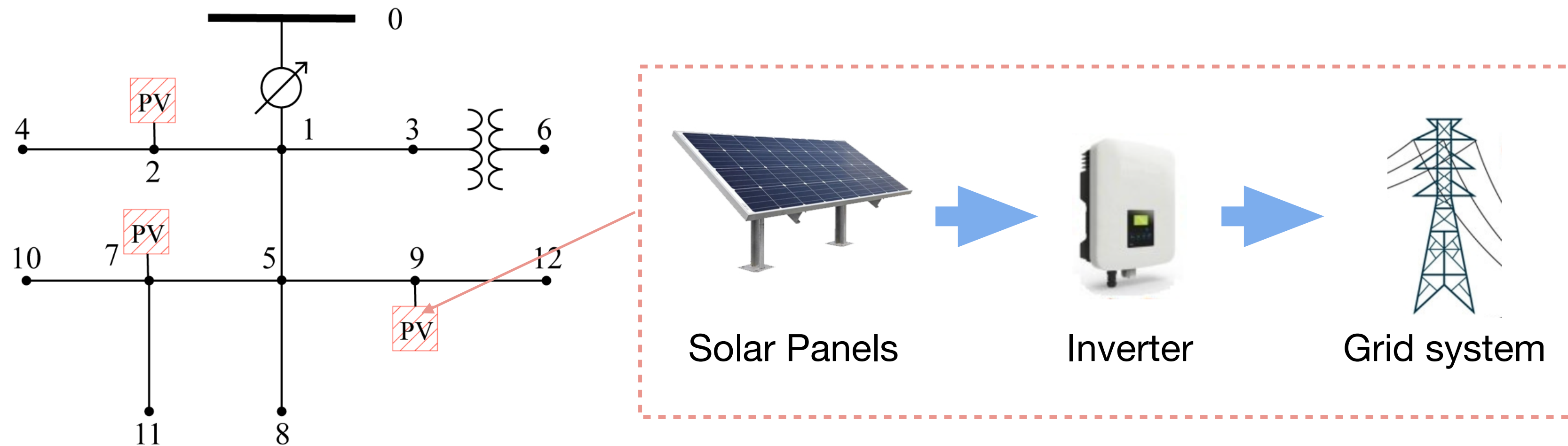
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# Background

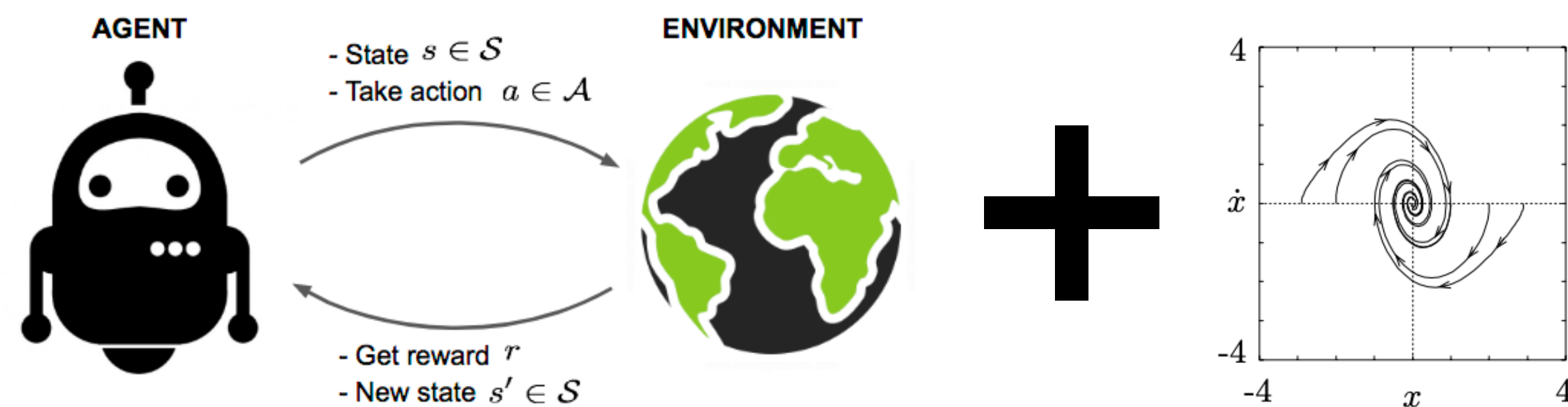
- Proliferation of distributed energy resources (DERs)
- Increasingly complex and rapid voltage violations
- Control of reactive power for voltage regulation
- Limited communication infrastructure ➡ decentralized controllers



# Overview of the proposed method

**Key Motivation:** Can we apply RL to voltage control with provable **stability guarantee**?

- Reinforcement learning provides a real-time control rule



- Lyapunov function gives a stability guarantee

# Problem Formulation

## Optimal Voltage Control Problem

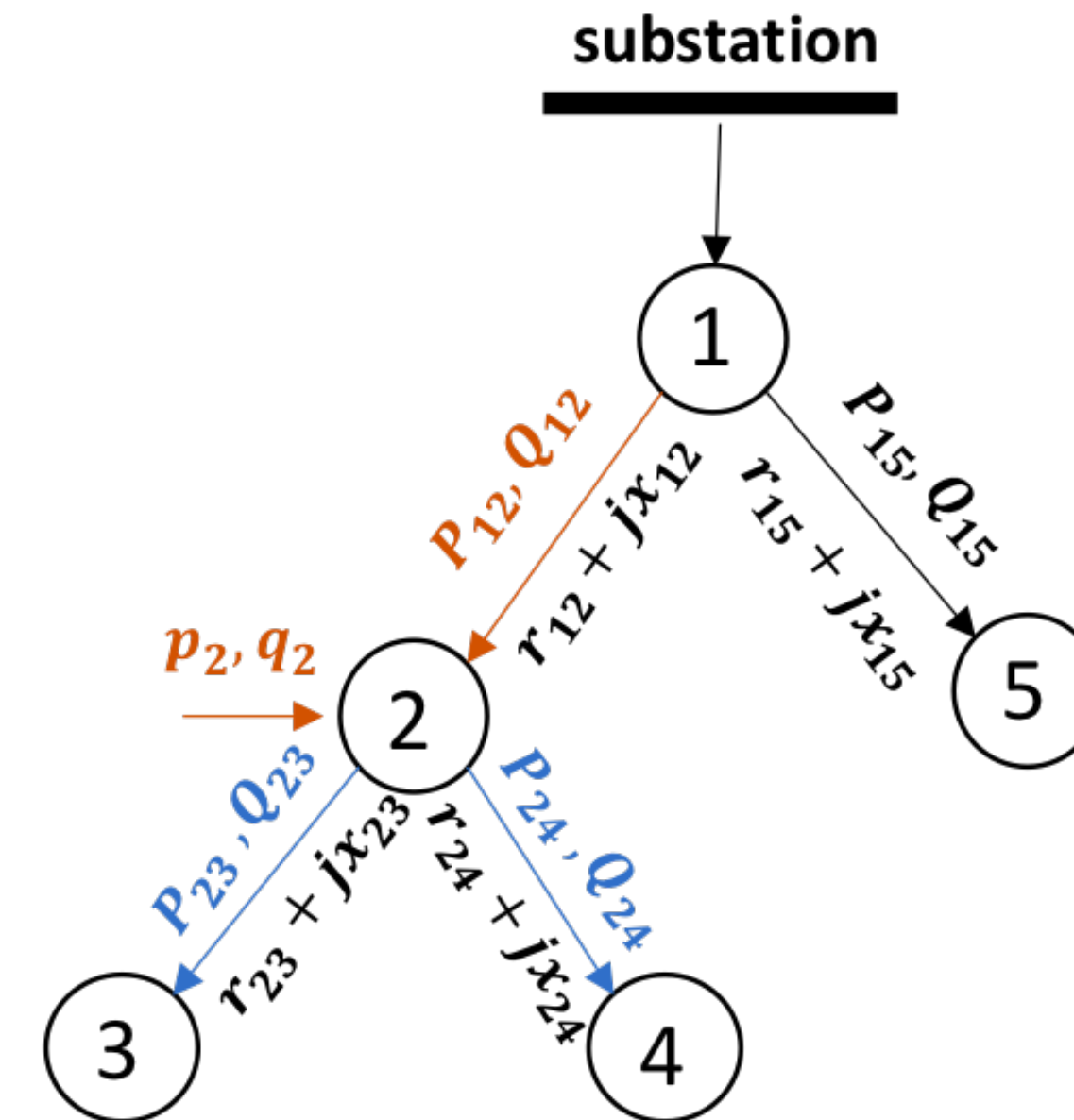
$$\min_{\theta} J(\theta) = \sum_{t=0}^H \gamma^t \sum_{i=1}^n c_i(v_i(t), u_i(t))$$

$$\mathbf{v}(t+1) = \mathbf{v}(t) + I_{\Delta T} X \mathbf{u}(t) = f_{\mathbf{u}}(\mathbf{v}(t))$$

$$u_i(t) = -g_{\theta_i}(v_i(t))$$

Neural Network  
Controller

voltage stability holds.



- Objective function:  $c_i(v_i(t), u_i(t)) = \eta_1 \|\max(v_i(t) - \bar{v}_i, 0) + \min(v_i(t) - \underline{v}_i, 0)\|_2^2 + \eta_2 \|u_i(t)\|_1$
- Update rule for q:  $q_i(t+1) = q_i(t) + u_i(t)$

# Voltage Stability Condition

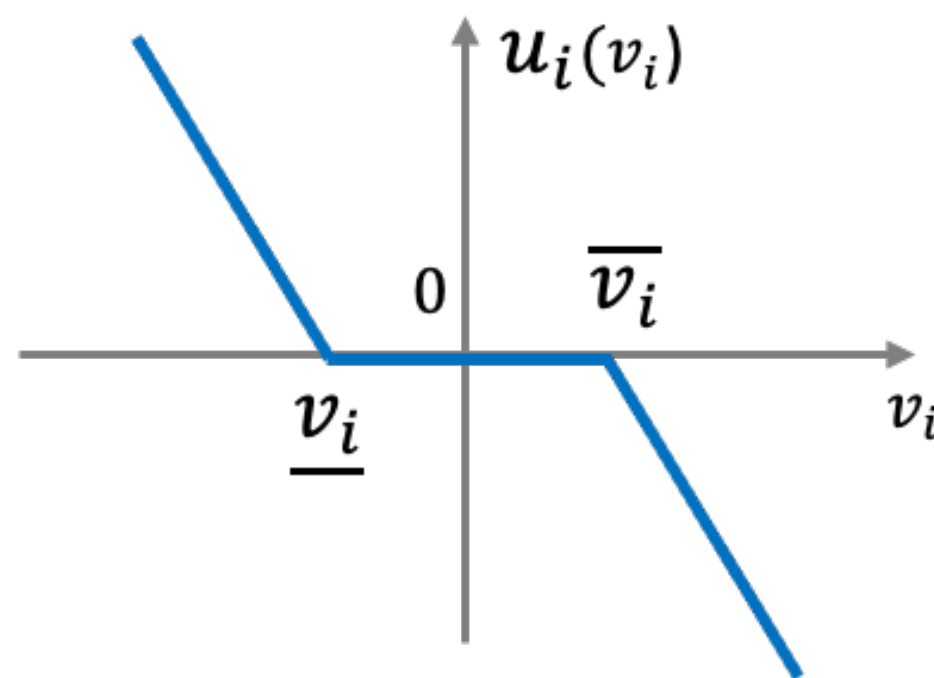
## Lyapunov Function

$$V(\mathbf{v}) = (\mathbf{v} - f_{\mathbf{u}}(\mathbf{v}))^{\top} X^{-1} (\mathbf{v} - f_{\mathbf{u}}(\mathbf{v}))$$

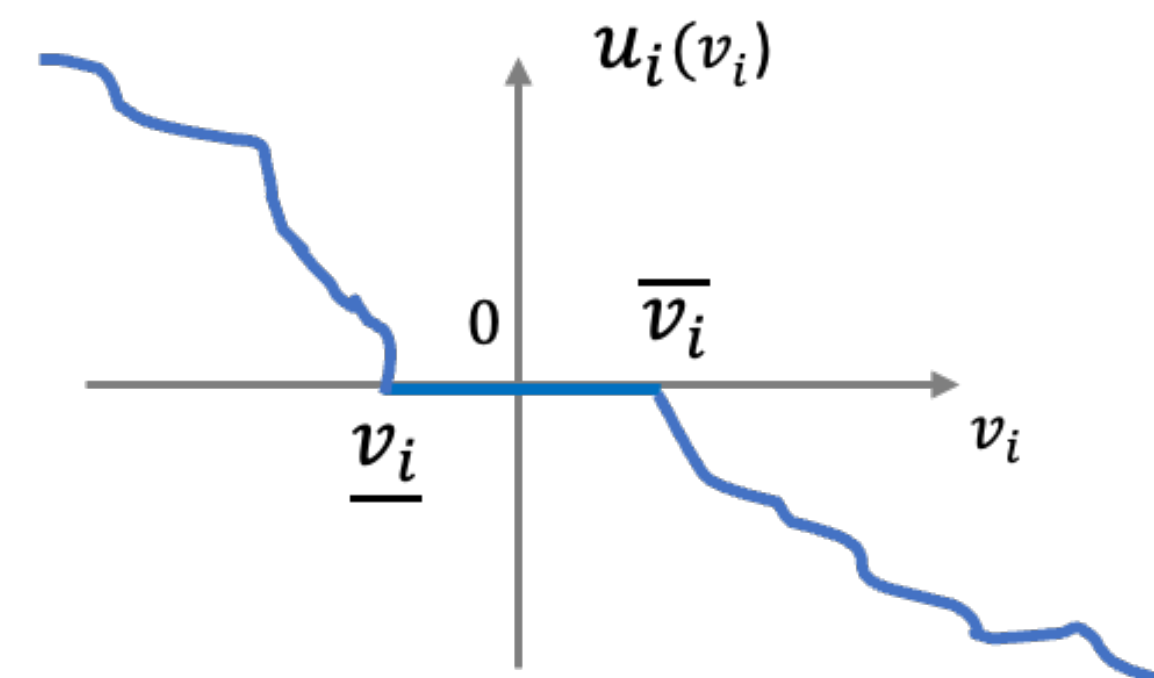
## Stability Condition

$$-\frac{2}{\Delta T} X^{-1} < \frac{\partial u}{\partial v} < 0$$

- Monotonicity ➡ Stability



Linear



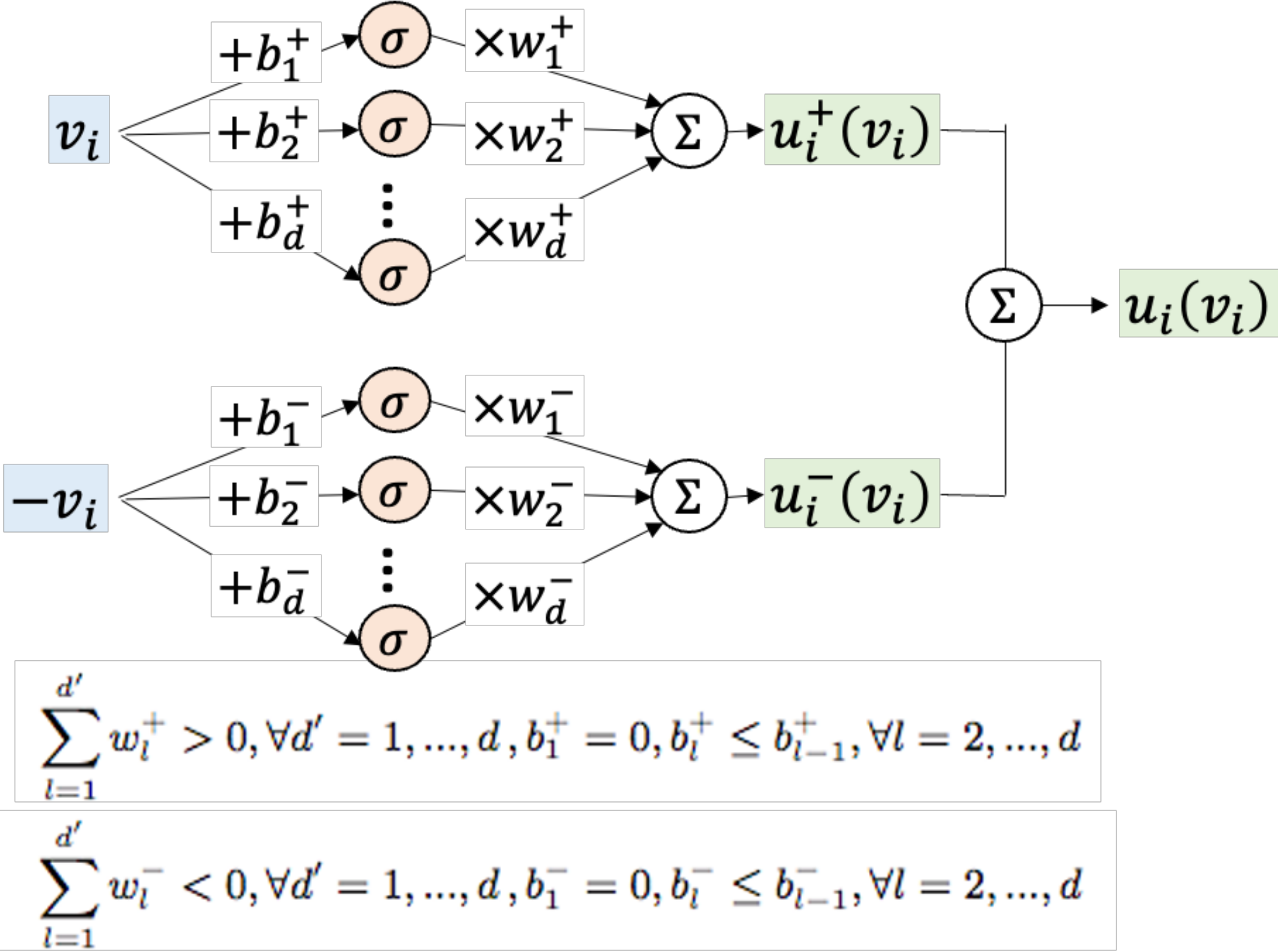
Monotone Neural Network



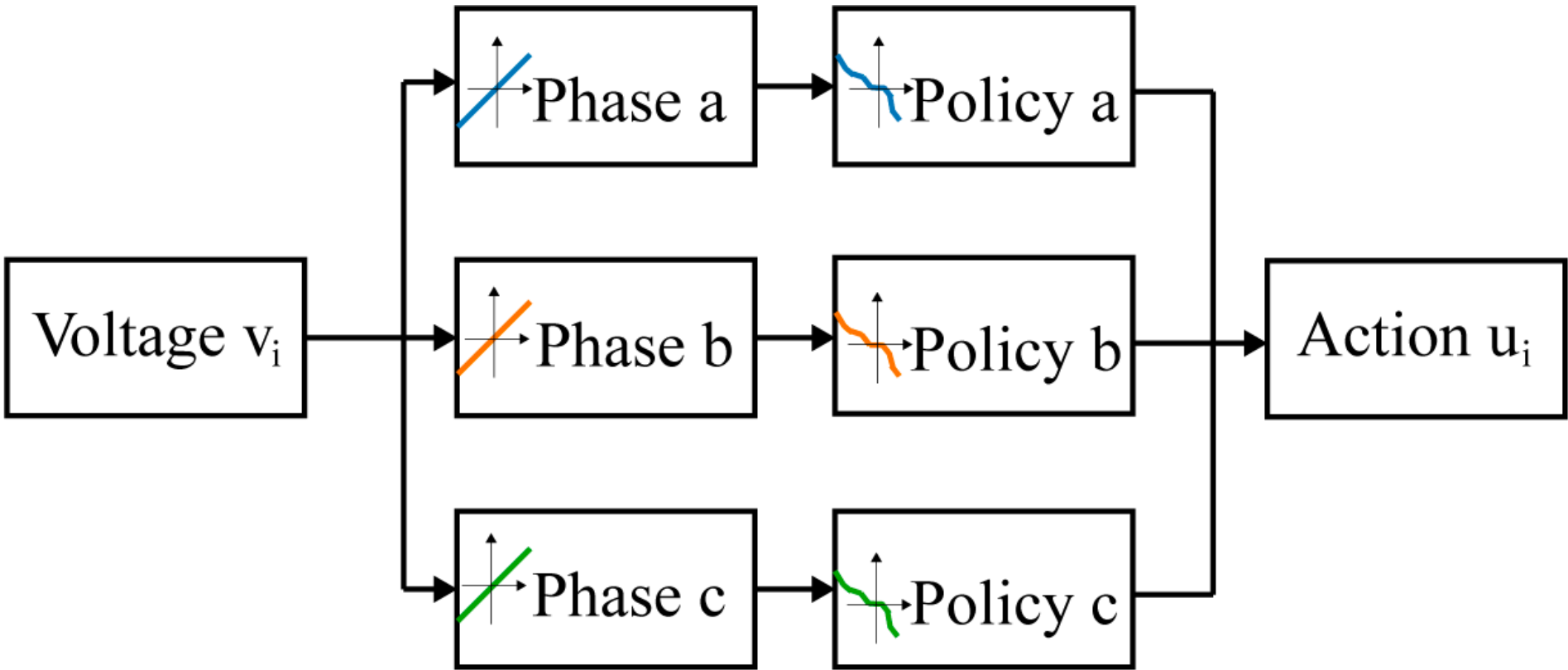
# Stable-DDPG

## Monotone Network Design

- Single-phase



- Three-phase



# Numerical result

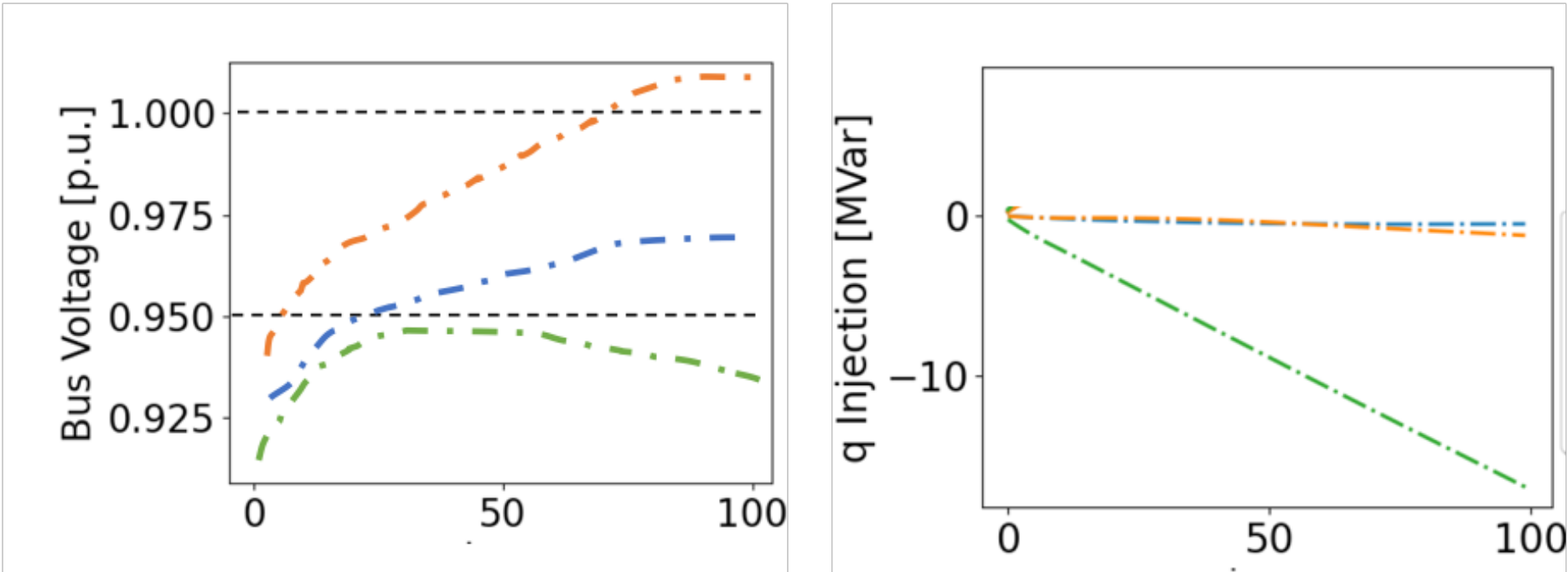
## IEEE 13-bus system

- Transient Performance

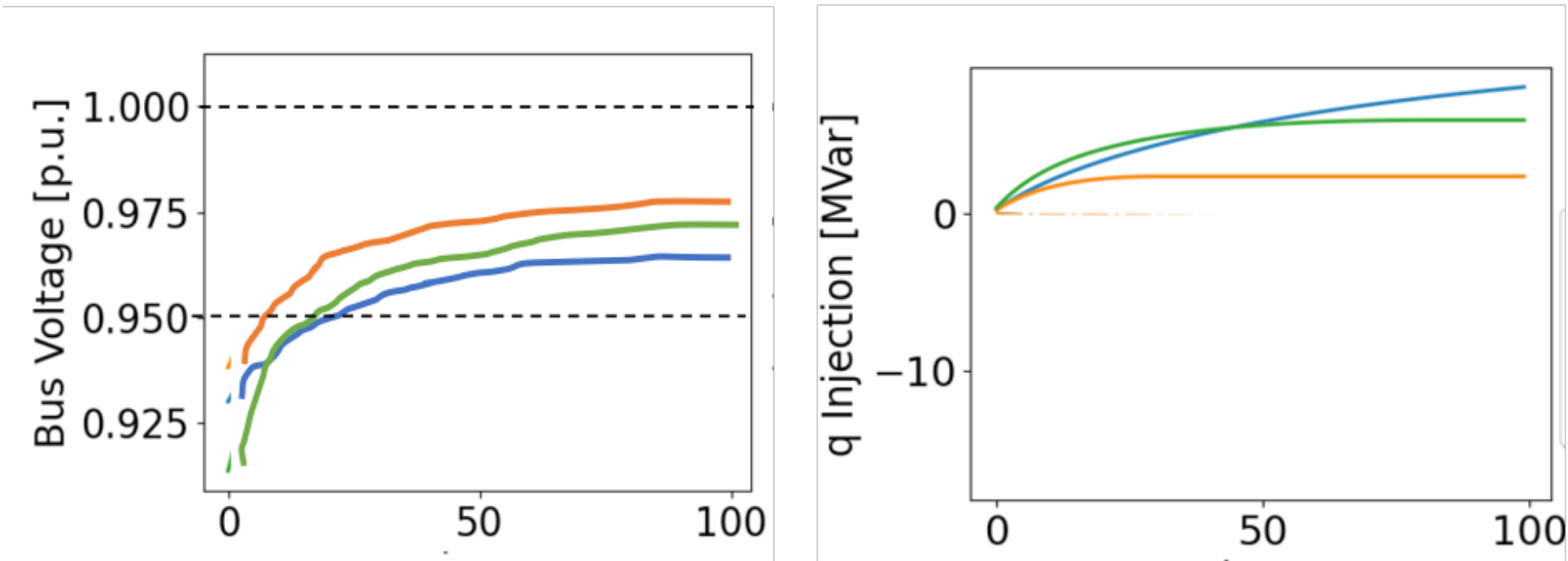
Method	Voltage recovery time (steps)		Reactive power (MVar)	
	Mean	Std	Mean	Std
Linear	5.31	3.19	8.22	10.72
<b>Stable-DDPG</b>	<b>4.47</b>	<b>2.43</b>	<b>6.75</b>	<b>8.08</b>
DDPG	6.61	20.67	30.20	120.24
DDPG*	2.31	1.18	3.65	3.21

The Stable-DDPG achieves best overall performance.  
It saves 16% of response time and 18% of reactive power consumption compared to the optimal linear policy.

## IEEE 123-bus system



(a) Dynamics of  $v$ (left) and  $q$  (right) for standard DDPG



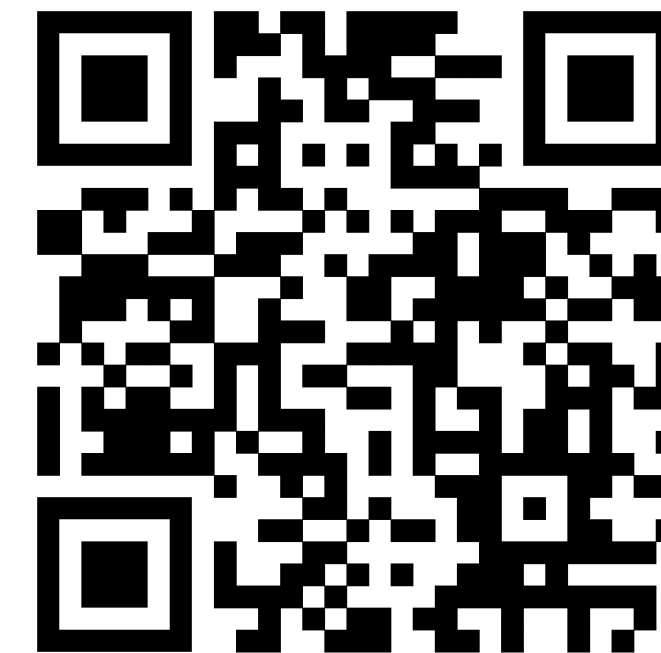
(b) Dynamics of  $v$ (left) and  $q$  (right) for Stable-DDPG



# Stable RL for Voltage Control

Thank you for listening

Code is available  
at GitHub, please  
scan the QR code



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