

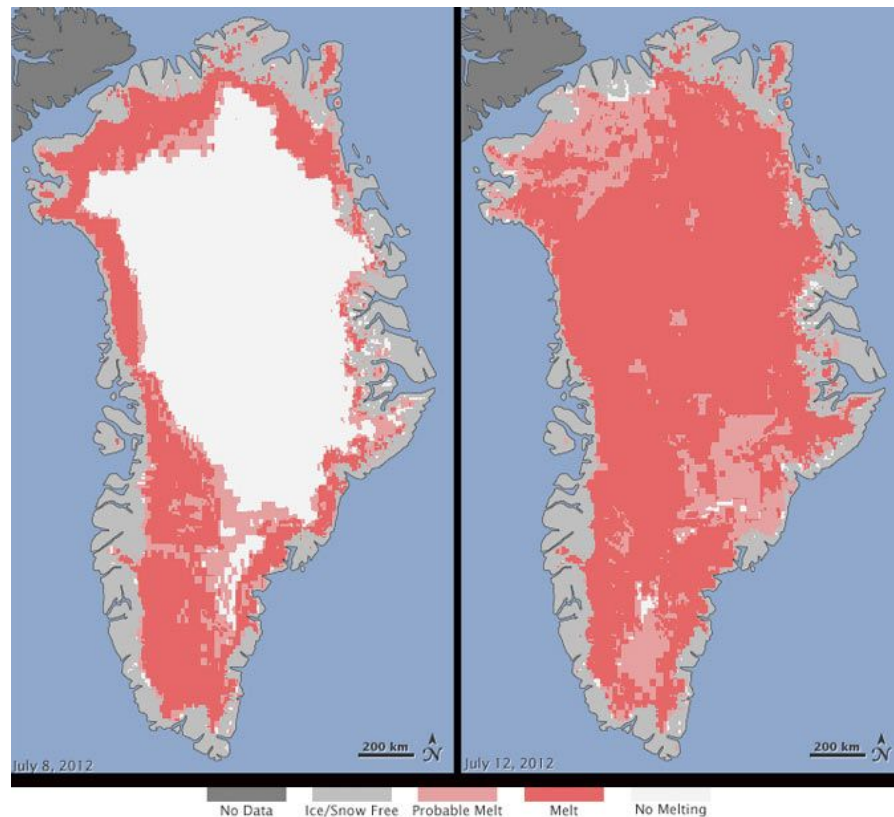
# **An Inversion Algorithm to Investigate the State of Friction at the Base of the Greenland Ice Sheet**

Aryan Jain, Jeonghyeop Kim, William Holt



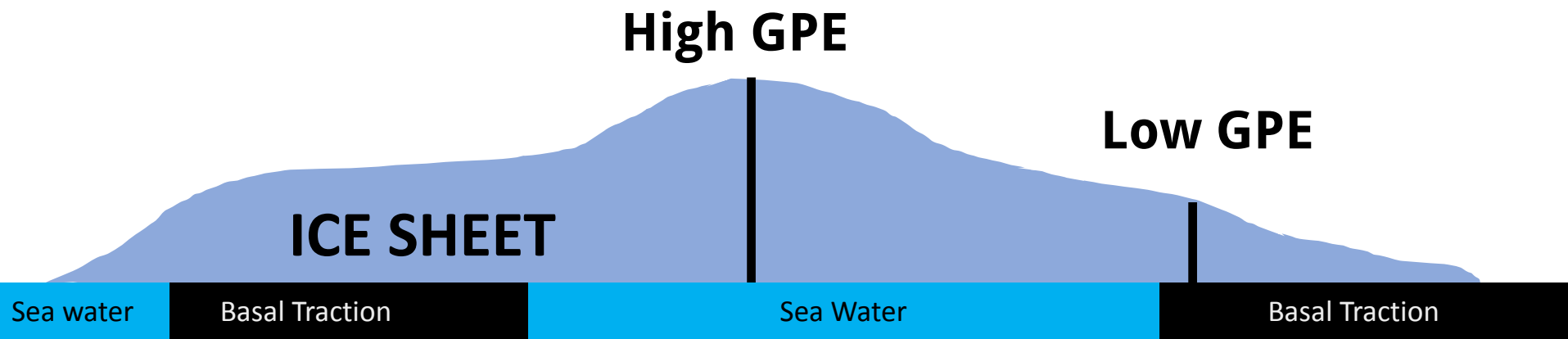
# Introduction

- The Greenland Ice Sheet (GrIS) has been melting at an alarming rate
  - Losing 200 Gt ice /year
  - Largest contributor to rising global sea levels
- To combat rising sea levels, it is imperative to understand these ice flow dynamics



# Previous Works

- Prior work analyzed GrIs flow leveraging Ice Thickness and associated gravitational potential energy (GPE) data
- GPE calculations were unable to account for basal tractions
- Our work developing an inversion algorithm to quantify basal tractions bridges this gap



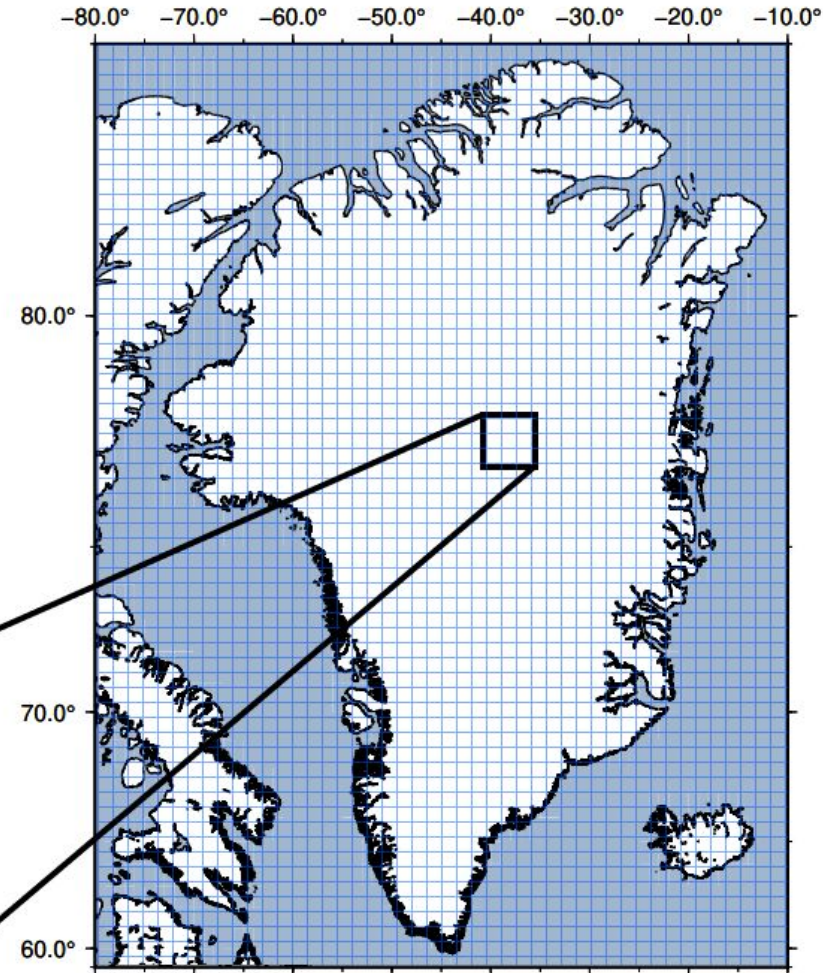
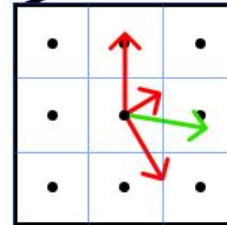
# Methods

- Our dataset is sourced from ETOPO1 topographical ice sheet and Sentinel-1 InSAR velocity measurements
- $\vec{d} = \bar{\bar{G}}\mathbf{m} = \mathbf{v}_{InSAR} - \mathbf{v}_{GPE}$ 
  - $\vec{d}$ : velocity field derived from velocity of InSAR – velocity of GPE
  - $\bar{\bar{G}}$ : Basis functions representing viscous thin-sheet responses caused by body-forces on the ice sheet
  - $\mathbf{m}$ : linear inversion model
- Goal to find best linear combination (  $\bar{\bar{G}}\mathbf{m}$  ) that predicts  $\vec{d}$

# Methods - $\bar{\bar{G}}$

- Partitioned Greenland into 1000  $2^\circ \times 2^\circ$  grid cells
- 3 Basis Functions for each grid cell:
  - $E_{xx}$  – Horizontal East and West effective body-forces
  - $E_{yy}$  – Horizontal North and South effective body-forces
  - $E_{xy}$  – Shear effective body-forces

■ : body-forces  
■ : ice-velocity

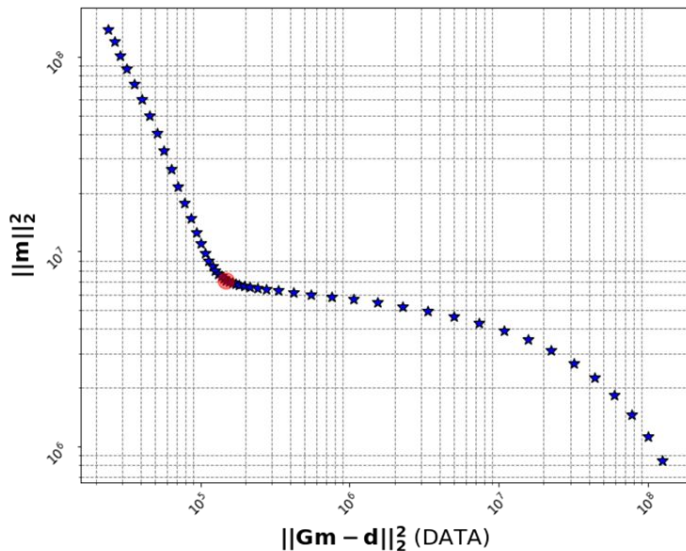


## Methods - $m$

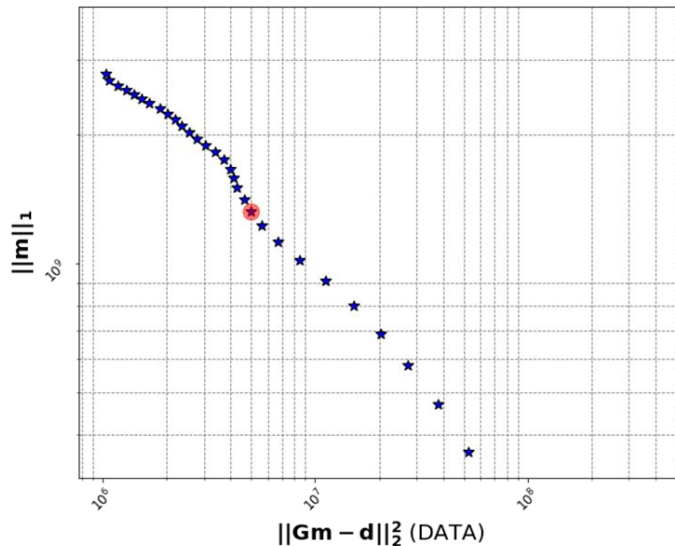
- Employed Linear Regression Algorithm from sklearn library
- Applied the Least Squares Method (LSM) with the Ridge (Tikhonov) and LASSO regularization to optimize our model
- LASSO Loss:  $\left\| \bar{\bar{G}}m - \vec{d} \right\|_2 + \alpha^2 \|m\|_1$
- Ridge Loss:  $\left\| \bar{\bar{G}}m - \vec{d} \right\|_2 + \alpha^2 \|m\|_2^2$
- Used the trade-off (L-curve) criterion to determine an “optimal” smoothing parameter

# Results

## Ridge Trade Off Curve



## LASSO Trade Off Curve



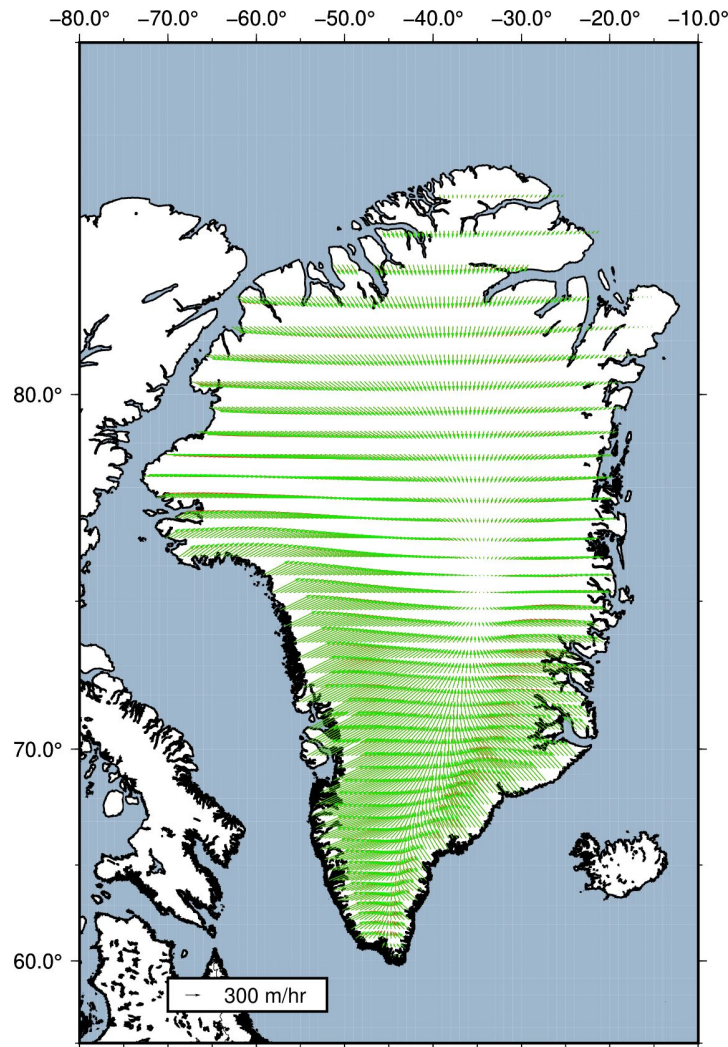
## Optimal Smoothing Parameters + Performance Metrics

	Best $\alpha$	$R^2$	RMSE	MAE
Ridge	<b>0.1520</b>	<b>0.9734</b>	<b>6.3651</b>	<b>4.3038</b>
LASSO	0.0324	0.9552	27.679	24.323



# Results

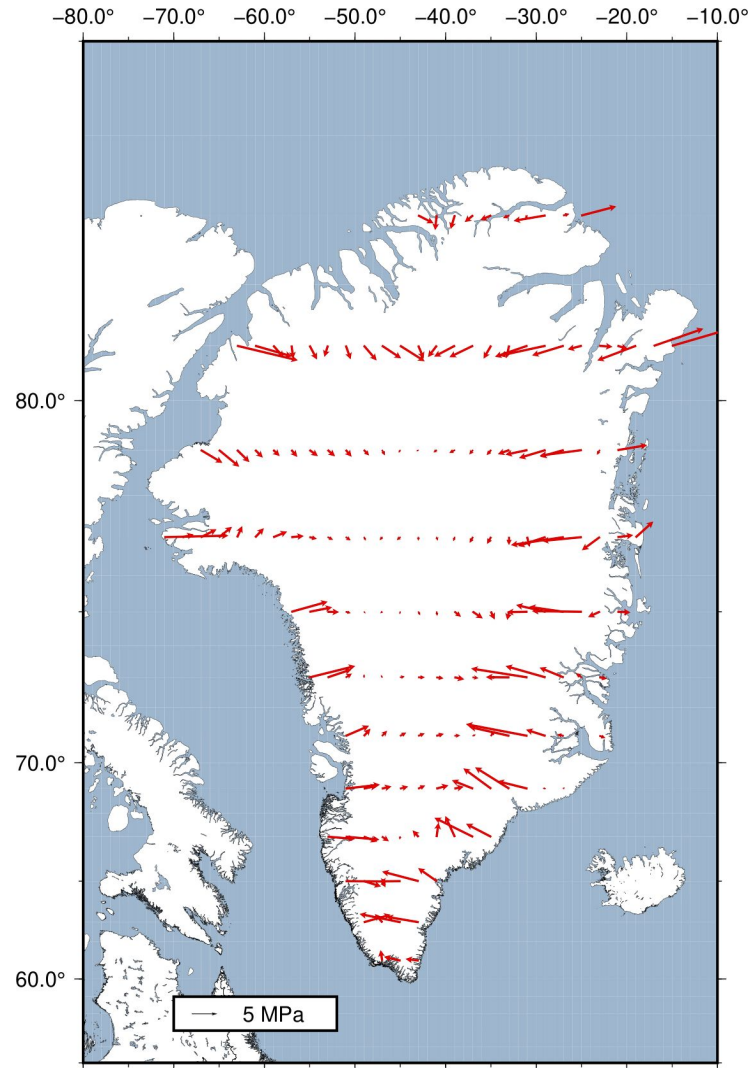
- Model predictions for GrIs horizontal velocity fields:
- InSAR velocities (red arrows) and model's predicted velocities (green arrows)
- Model achieves near identical fit
- Discrepancies most prevalent near edges as a result of grid cell resolution





# Results

- Model Basal Traction Predictions:
- Uncovers magnitudes and distributions of basal tractions across GrIs
- Basal Traction lie around GrIs coastline
- Work enables scientists to relate changes in basal tractions to change in ice velocities and flux



# Conclusions

- Successfully predicted horizontal velocity field and associated basal tractions
- Enhances knowledge of ice flow, uncovering relationships between basal traction, velocity fields, and ice flux
- Demonstrates the promise of applying ML to gain a deeper understanding of ice sheets, giving us valuable insight towards rising sea levels needed in the fight against climate change.
- Future Works will explore use of deep learning and applications to Antarctic