

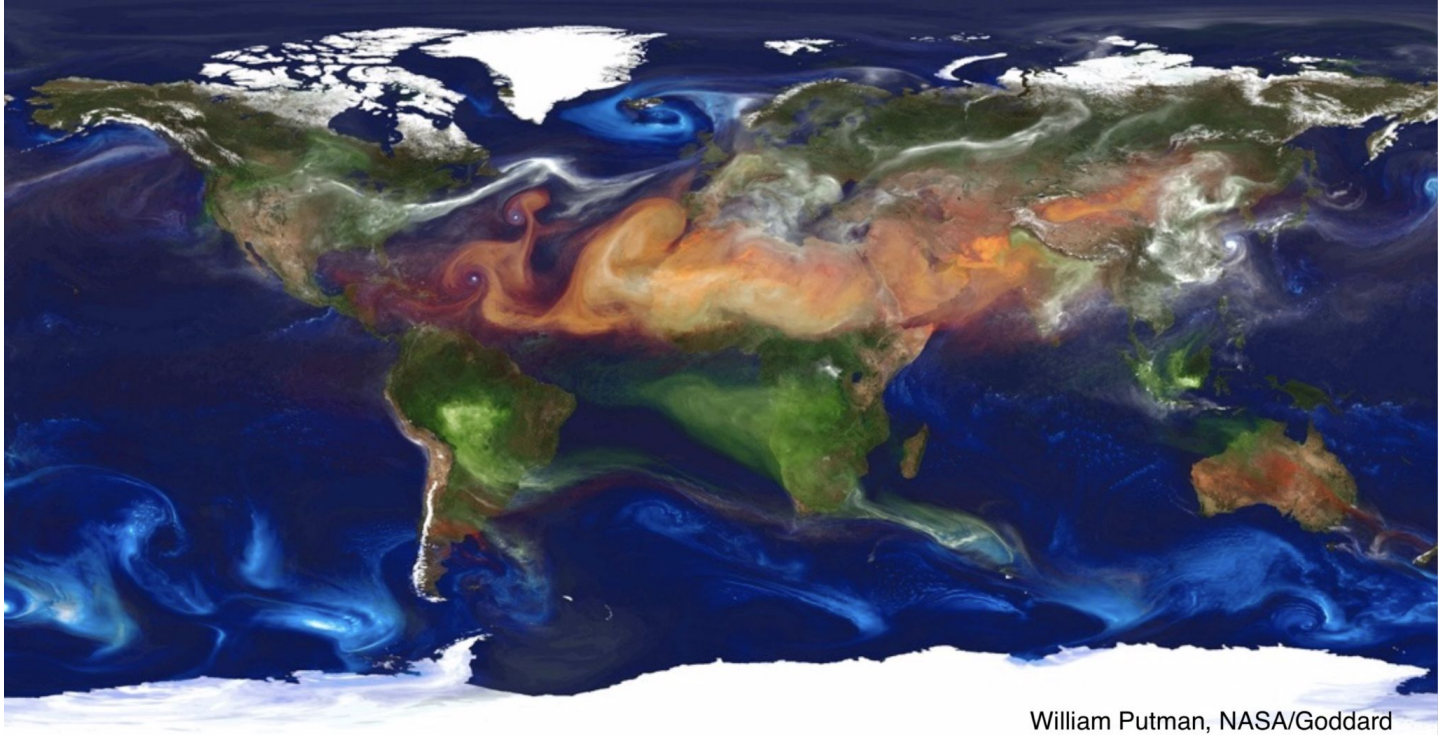
Reconstructing Aerosol Vertical Profiles with Aggregate Output Learning

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This project receives funding from the European Union's Horizon 2020 research and innovation programme under Marie Skłodowska-Curie grant agreement No 860100.

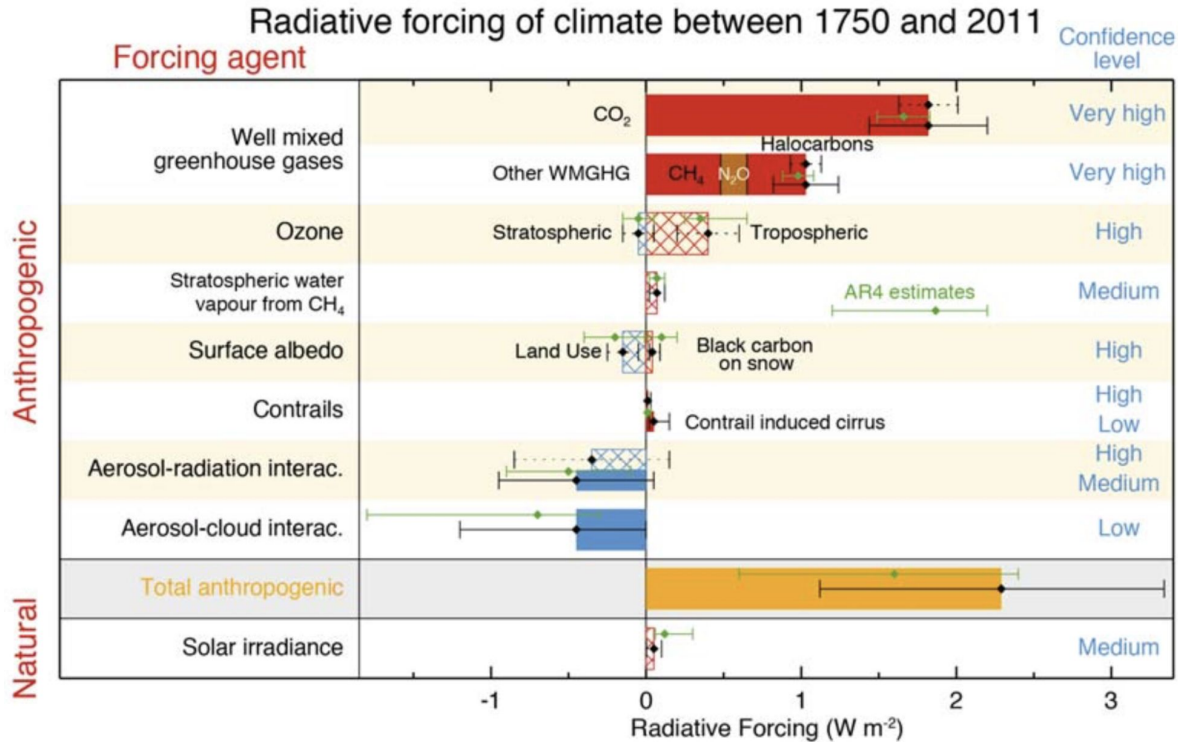
Motivation



GEOS-5 10km resolution

Red: Dust Blue: Sea Salt Green: Smoke White: Sulfate

Motivation

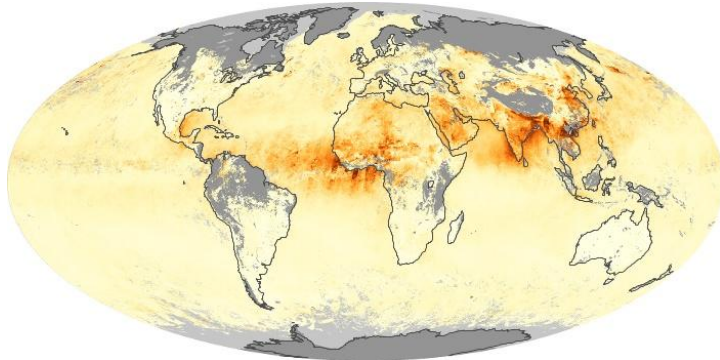


IPCC 2013

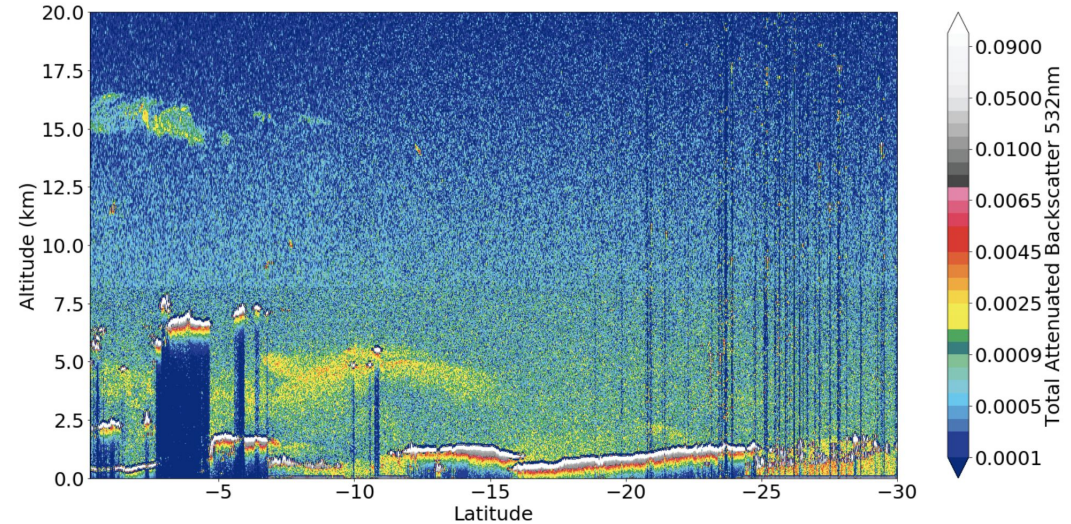
Motivation

2D proxies (vertically aggregated data) often insufficient to understand aerosol distribution

e.g. aerosol optical depth from satellites
$$\text{AOD} = \int_0^H b_{\text{ext}}(h)dh$$



MODIS AOD



CALIOP lidar vertical profile ('scene')

Problem Statement

General setup:

- Collection of bagged observations: $\{\{x_j^{(i)}\}_{i=1}^H, y_j, z_j\}_{j=1}^n$
- Function to disaggregate: $f : \mathbb{R}^{d_x} \rightarrow \mathbb{R}$
- Aggregation operator over column height: $\text{Agg}_j : f \mapsto \int_{j^{\text{th}} \text{column}} f(x) \, dh(x)$
- Aggregate observation model:

$$z_j = \text{Agg}_j(f) + \varepsilon_j$$

Specific problem to develop a proof of concept for the methodology:

Reconstruct vertical profiles of sulfate concentrations from aggregated column mass density + chemical and meteorological covariates

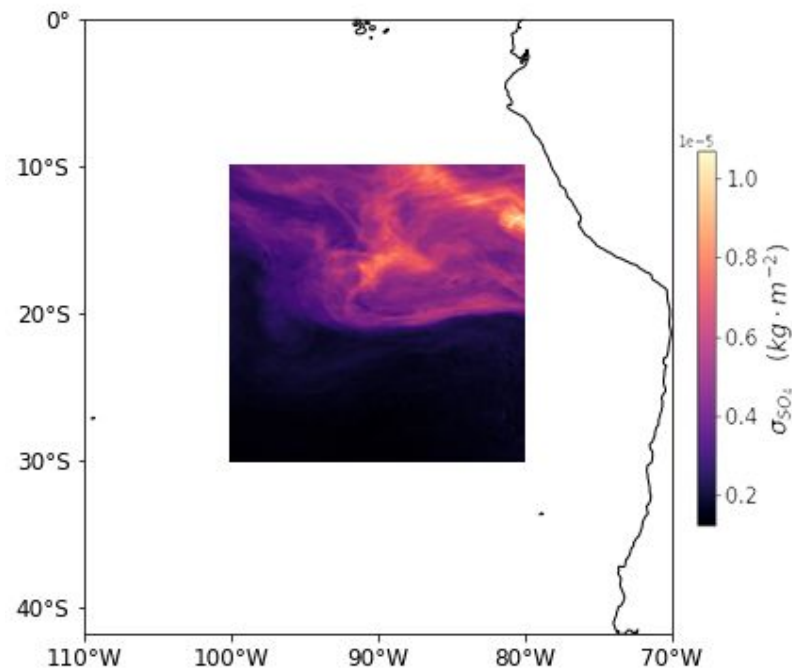
$$\sigma_{\text{SO}_4} = \int_0^H [\text{SO}_4](h) \, dh$$

Dataset

[NASA's GEOS-5 Nature Run](#) output used as dataset basis.

	Name	Notation	Units
2D	SO ₄ column density	σ_{SO_4}	kg·m ⁻²
	Liquid water path	LWP	kg·m ⁻²
3D	SO ₄ mass mixing ratio	r_{SO_4}	kg·kg ⁻¹
	SO ₂ mass mixing ratio	r_{SO_2}	kg·kg ⁻¹
	Relative Humidity	RH	1
	Air temperature	T	K
	Vertical velocity	w	m·s ⁻¹
	Cloud liquid water	q	kg·kg ⁻¹
	Moist air density	ρ	kg·m ⁻³

Table 1. Dataset variables, “2D” corresponds to variables indexed by time, latitude and longitude while “3D” corresponds to variables that also have a height dimension.



Initial Solutions - Baseline 1

Input 3D covariates : $x = (\text{latitude, longitude, altitude, } r_{\text{SO}_2}, \text{RH}, T, w, q)$

Objective :

$$\min_f \sum_{i=1}^n \left(\sigma_{\text{SO}_4 i} - \int_{i^{\text{th}} \text{ column}} f(x) dh(x) \right)^2$$

Hypothesis :

$$f(x) = \beta^\top x$$

Solution : Closed form ridge regressor of column-aggregate inputs against AOD

Initial Solutions - Baseline 2

Input 3D covariates : $x = (\text{latitude, longitude, altitude, } r_{\text{SO}_2}, \text{RH}, T, w, q)$

Input 2D covariates : $y = (\text{latitude, longitude, } \sigma_{\text{SO}_4}, \text{LWP})$

Step 1 : Fit $g : y_i \mapsto \int_{i^{\text{th}} \text{ column}} f(x) dh(x)$

Step 2 : $\min_f \sum_{i=1}^n (\sigma_{\text{SO}_4 i} - g(y_i))^2$

Hypothesis : $f(x) = \beta^\top x$

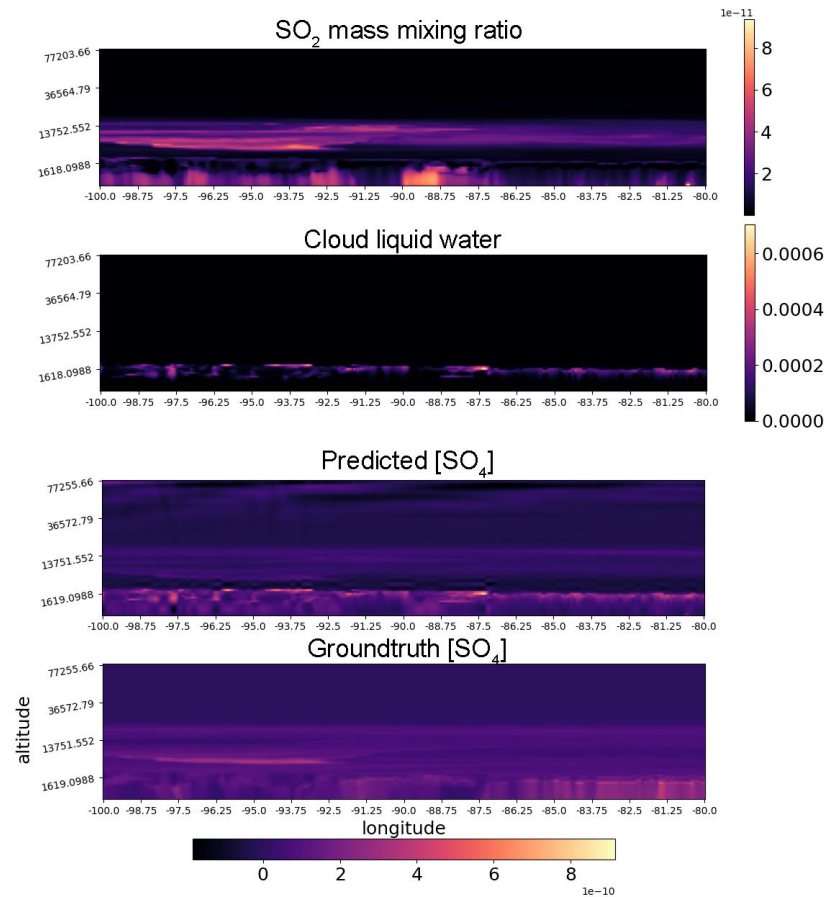
$g(y) = \gamma^\top y$

Solution : Closed form two-stage ridge regressor

Experiments

		RIDGE	TWO-STAGE
2D	RMSE (10^{-6})	3.47	3.52
	MAE (10^{-6})	3.39	3.39
	Corr. (%)	93.5	87.5
3D	RMSE (10^{-10})	2.71	2.50
	MAE (10^{-10})	1.07	1.10
	Corr. (%)	62.5	63.9

Table 2. Evaluation scores on vertical profile reconstruction; “2D” refers to evaluation against aggregate σ_{SO_4} targets used for training; “3D” refers to evaluation against vertical groundtruth



Discussion & future work

- Two-stage regression shows a slight increase in performance over simple kernel ridge regression with metrics used
- Unclear why the influence of SO₂ profiles (important sulfate precursor gas) on predictions varies in experiments
- Metrics more suited to the problem should be developed
- Next step: use specialised aerosol models with lidar simulator and develop kernel-based model to tackle the AOD disaggregation problem:

Reconstruct vertical profiles $b_{\text{ext}}(h)$ from aggregated observations of the AOD and chemistry + meteorological covariates

Code and data available at:

<https://github.com/shahineb/aerosols-vertical-profiles>